

A Stretching Algorithm for Parallel Real-time DAG Tasks on Multiprocessor Systems

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Presentation Outline

- General Introduction
- Related Work & Problem Description
- DAG Stretching Algorithm
- Resource Augmentation Bound for global preemptive EDF
- Simulation-based Evaluations
- Conclusion and Perspective

General Introduction

- **Hard Real-time Systems**

- Failure in respecting timing characteristics of the real-time system leads to catastrophic results.

- **Multiprocessor Systems**

- execution platform consists of homogeneous unit-speed processors.

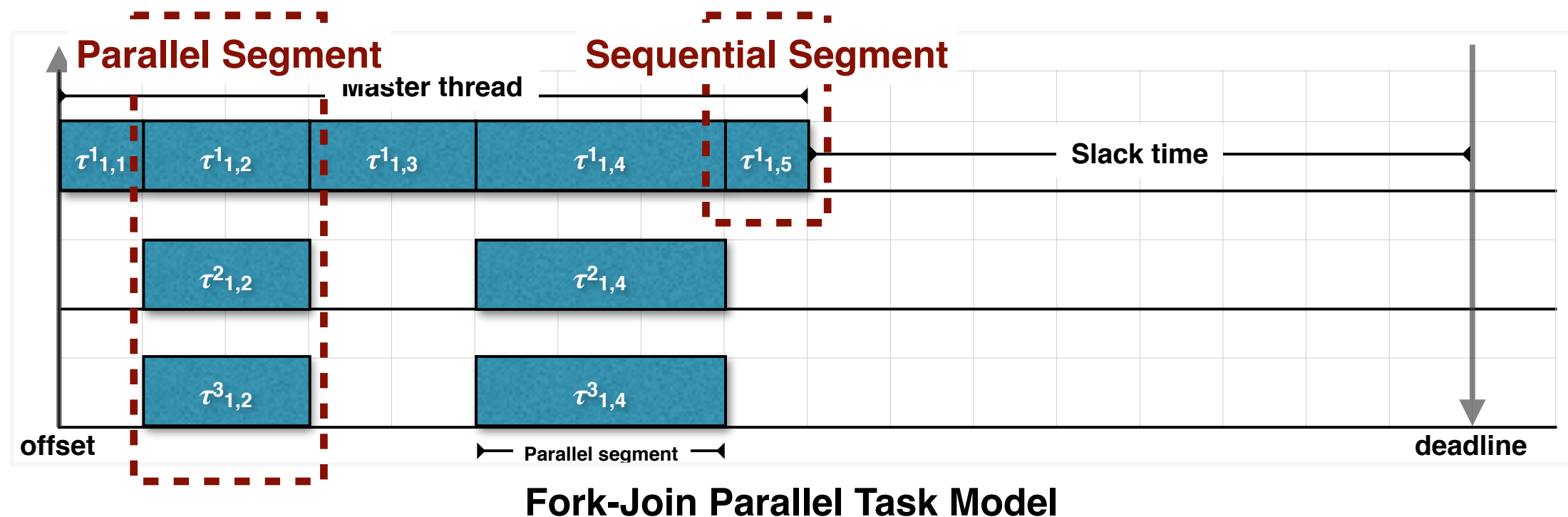
- **Global Preemptive Scheduling**

- the execution of a job can be interrupted by higher priority jobs, and job migration is allowed between processors.

Software Parallelism

- **Parallel programming** is proposed as an evolution of **software** so as to get advantage of **multiprocessor architecture**.
- **Parallel programming APIs**: OpenMP, pThreads
- Many **real-time parallel task models**: Fork-join (FJ) and Multi-Threaded Segment Model, Directed Acyclic Graphs (DAG).

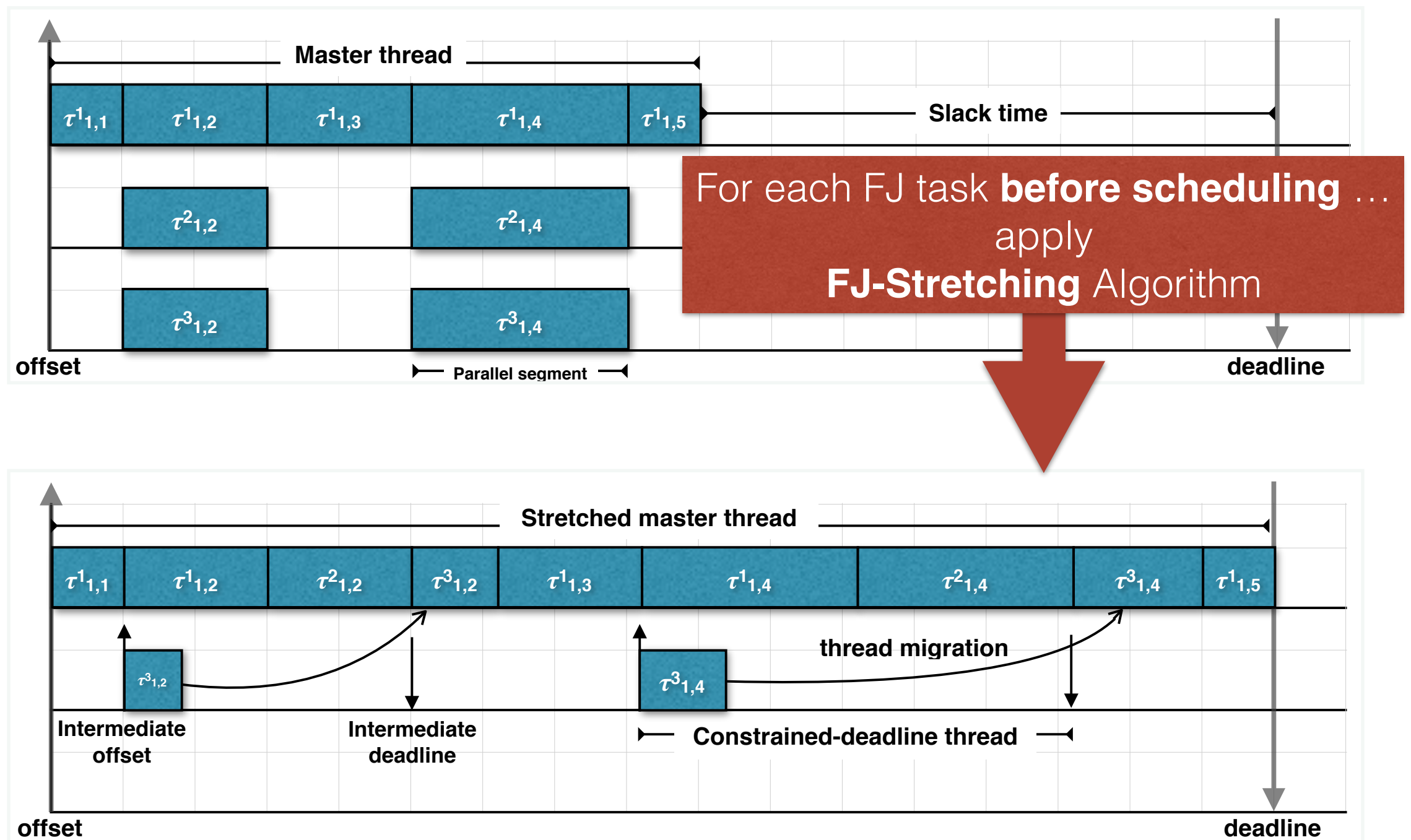
Related Work: FJ-Stretching Algo.



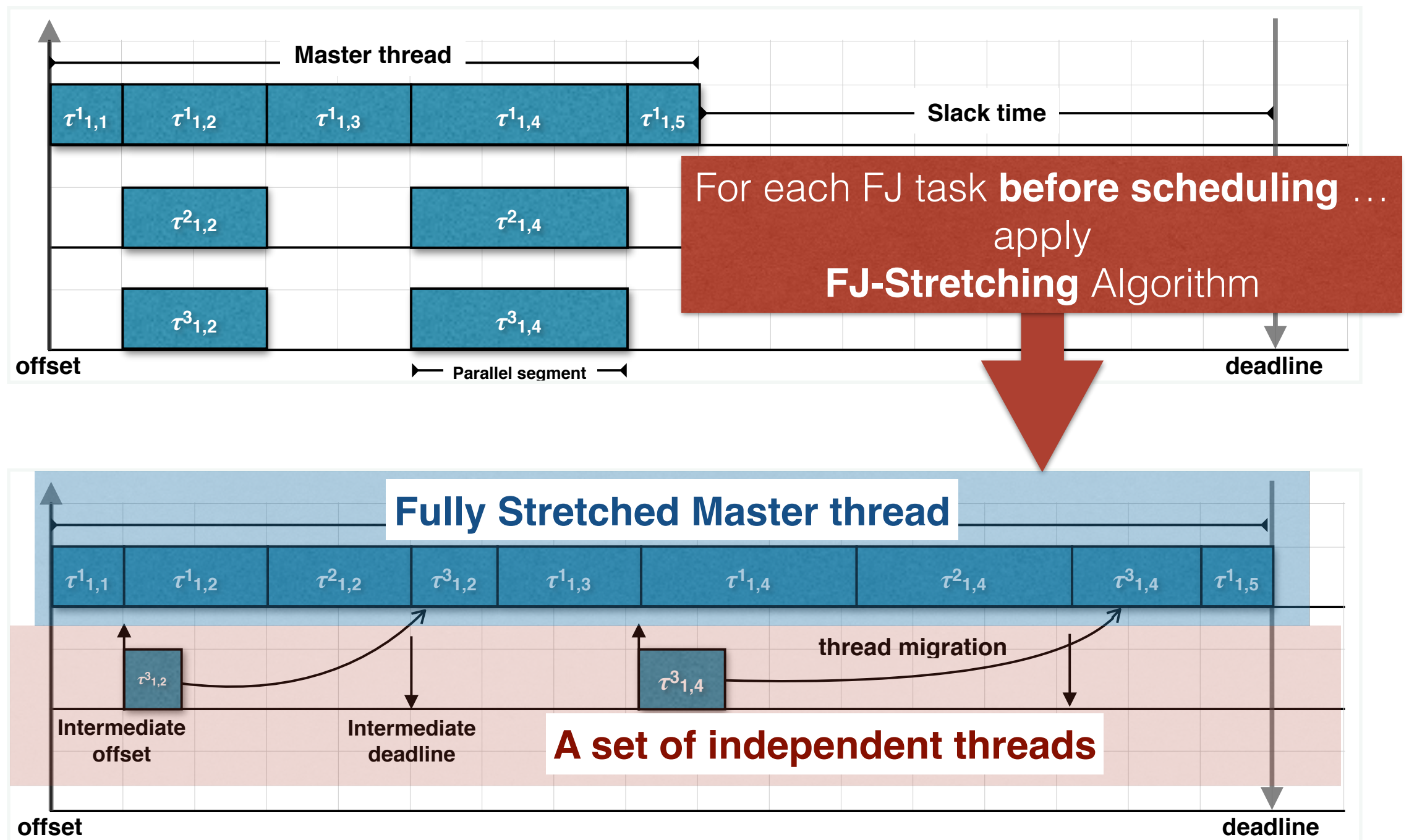
Fork-join task sets on multiprocessor systems can have schedulable utilization bounds slightly greater than and arbitrarily **close to uniprocessor schedulable utilization bounds**. From the perspective of schedulability, it is therefore desirable to **avoid such task structures** as much as possible.¹

[1] "Scheduling Parallel Real-Time Tasks on Multi-core Processors". Lakshmanan et al., ECRTS 2010

Related Work: FJ-Stretching Algo.

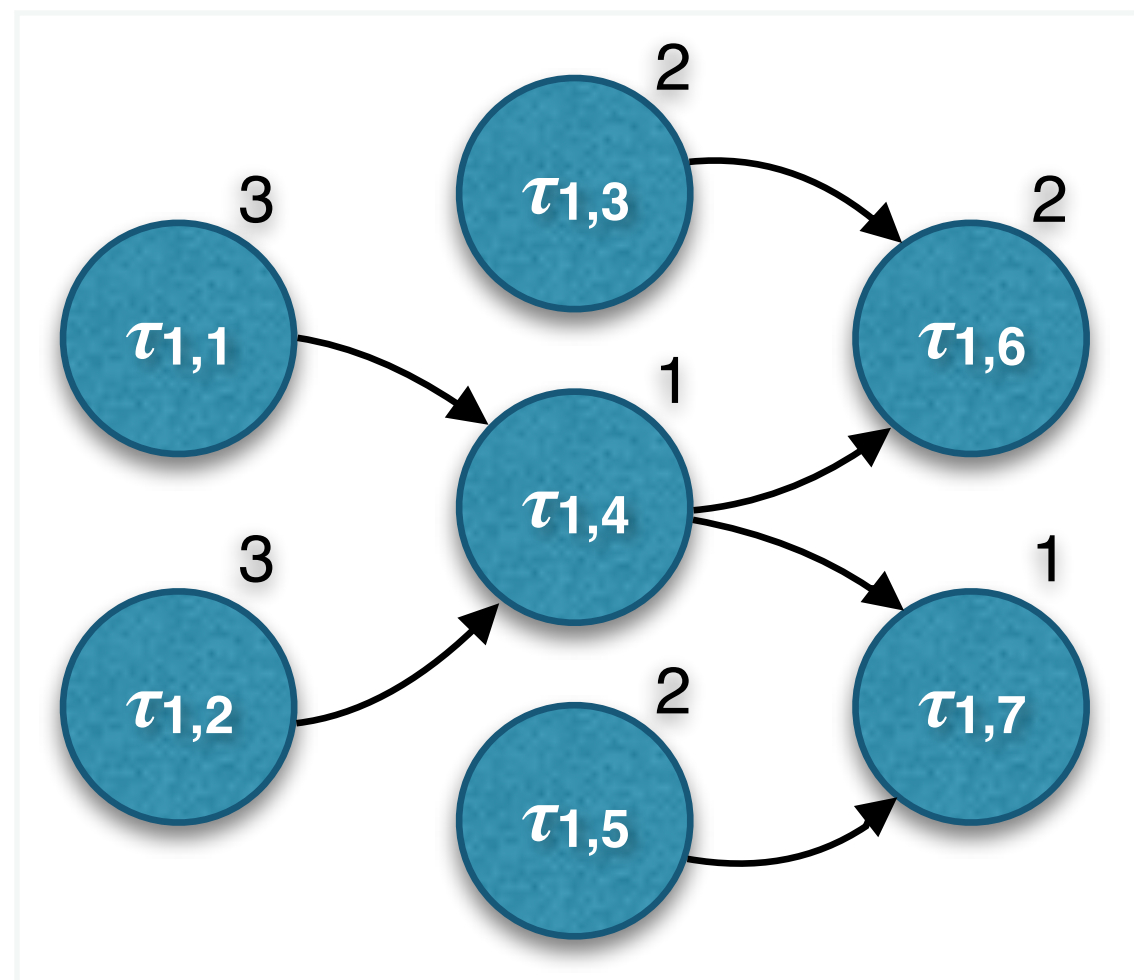


Related Work: FJ-Stretching Algo.



Contribution: DAG-Str Algorithm

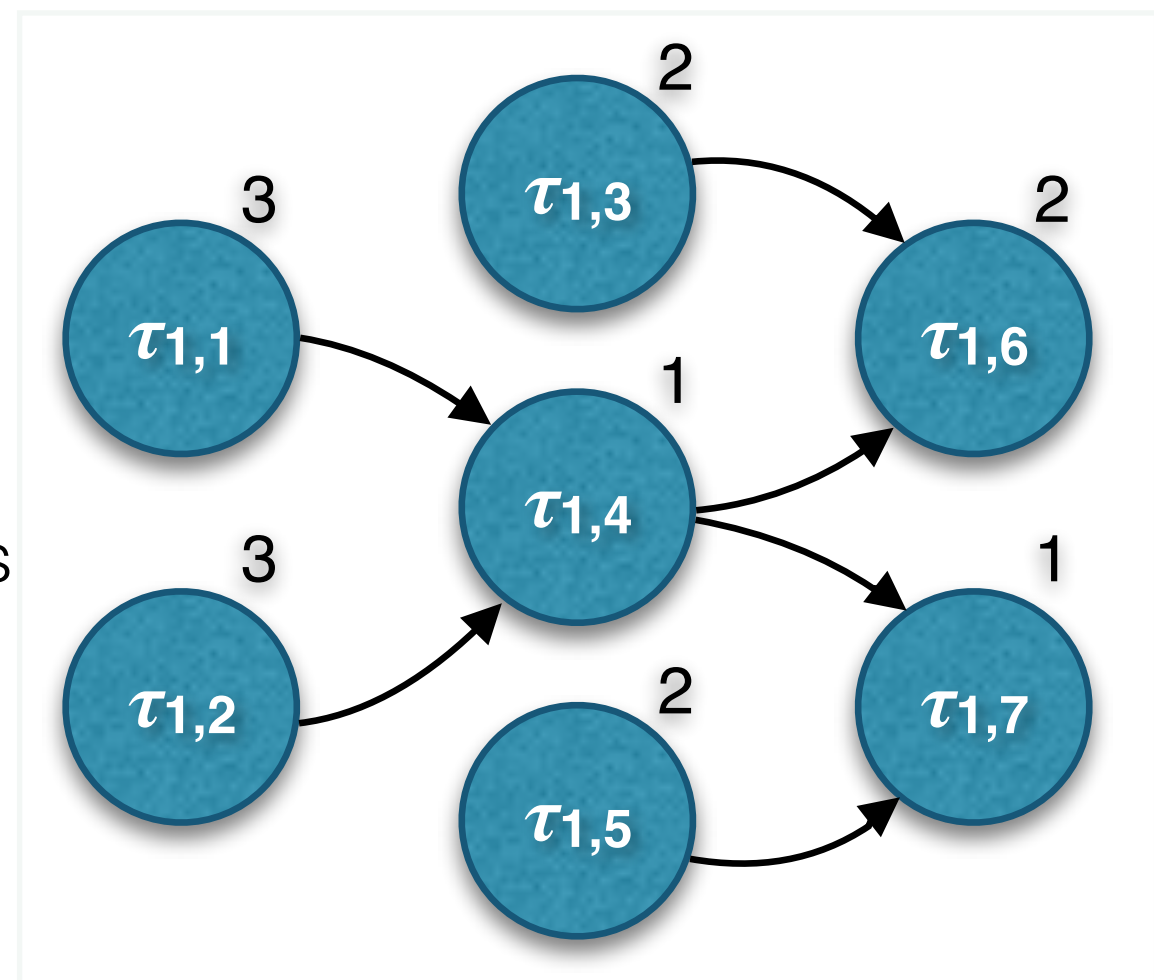
We propose a **DAG-Str (DAG Stretching) Algorithm**



Contribution: DAG-Str Algorithm

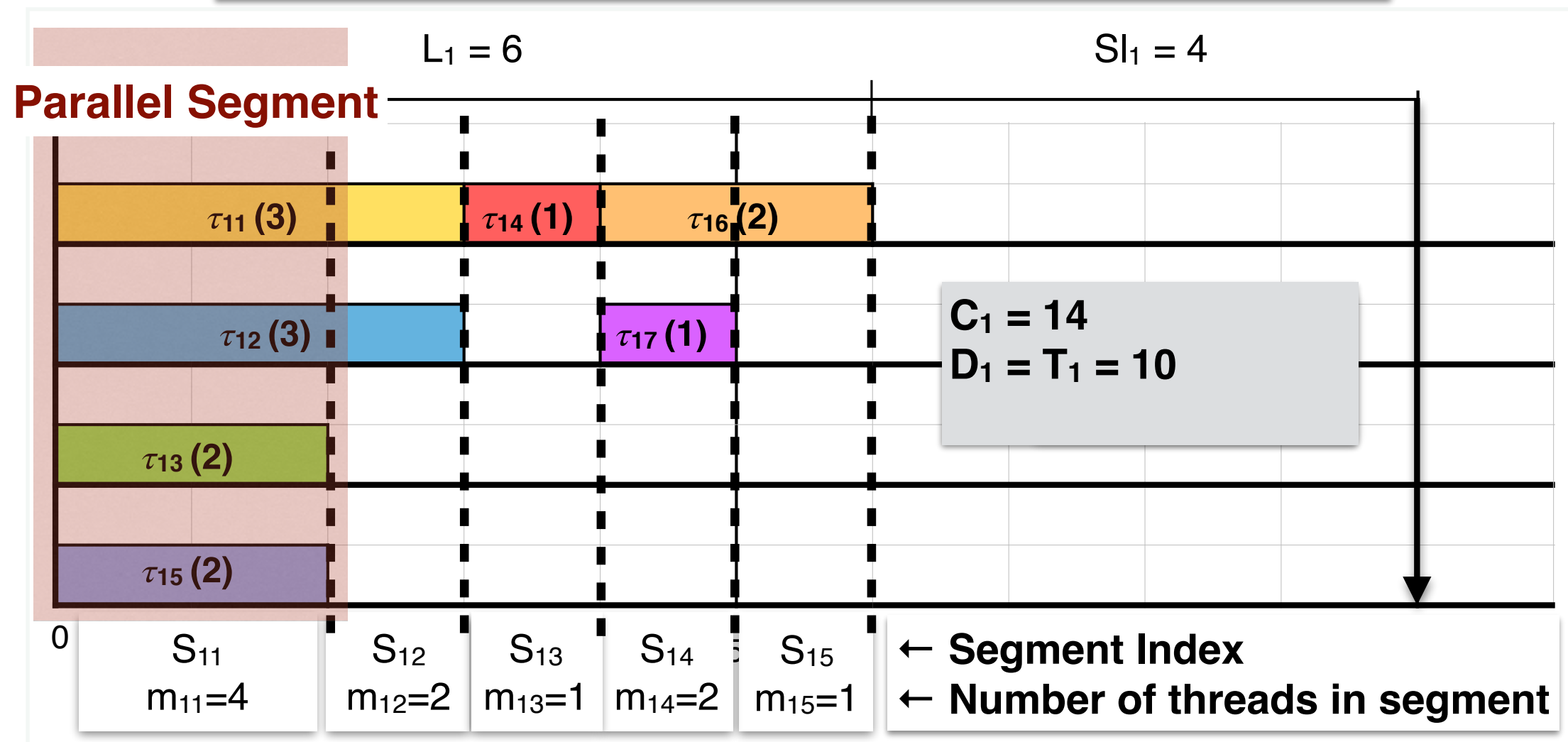
We propose a **DAG-Str (DAG Stretching) Algorithm**

- A DAG task (periodic, implicit-deadline):
 - Set of subtasks with specific WCETs
 - Set of precedence constraints between subtasks
 - timing parameters: offset, relative deadline, period



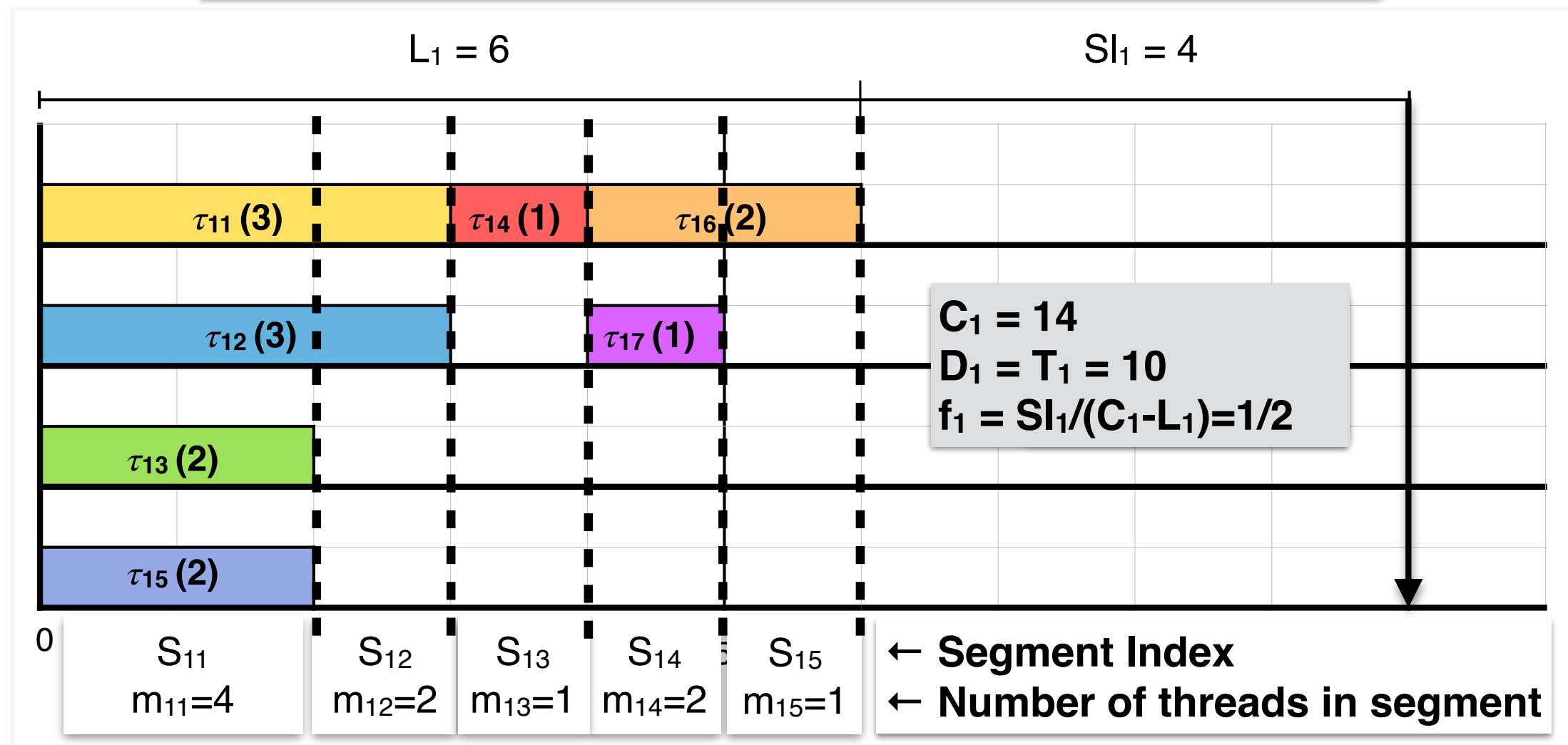
DAG-Str Algorithm

Multi-Threaded Segment Form of DAG task



DAG-Str Algorithm

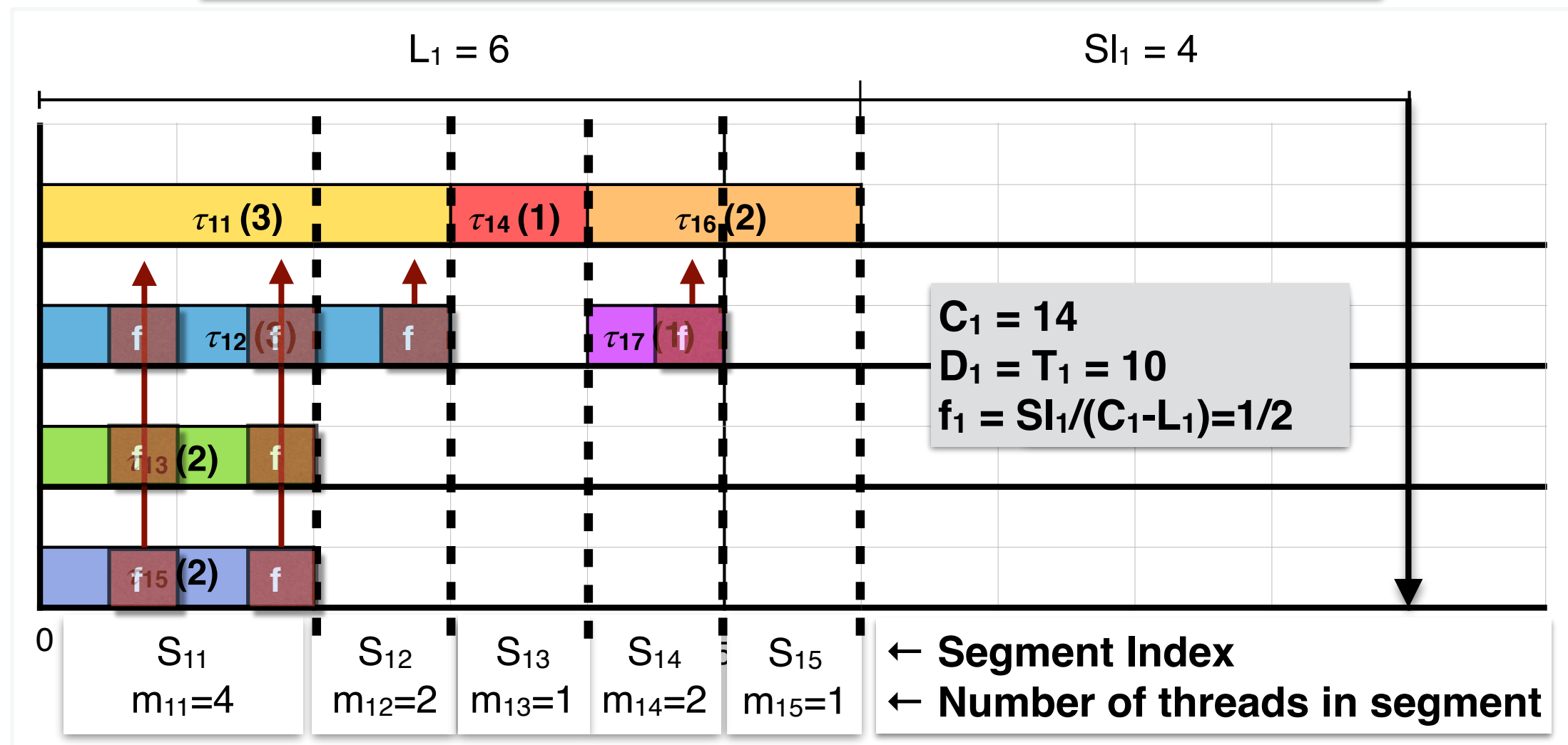
Calculate a unit factor f_1 of the DAG task



Uniform slack filling on a **Thread-level**

DAG-Str Algorithm

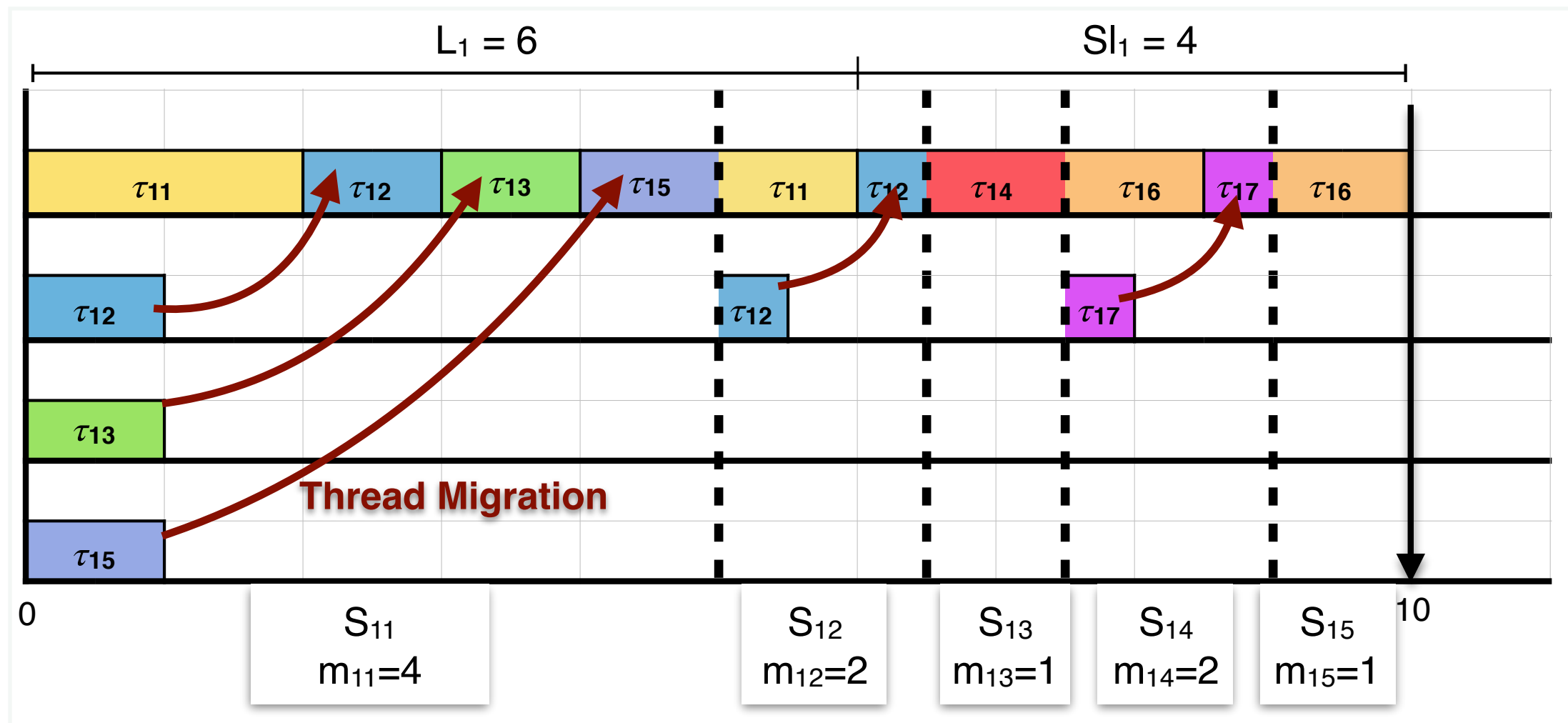
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Uniform slack filling on a **Thread-level**

DAG-Str Algorithm

Calculate a unit factor f_1 of the DAG task

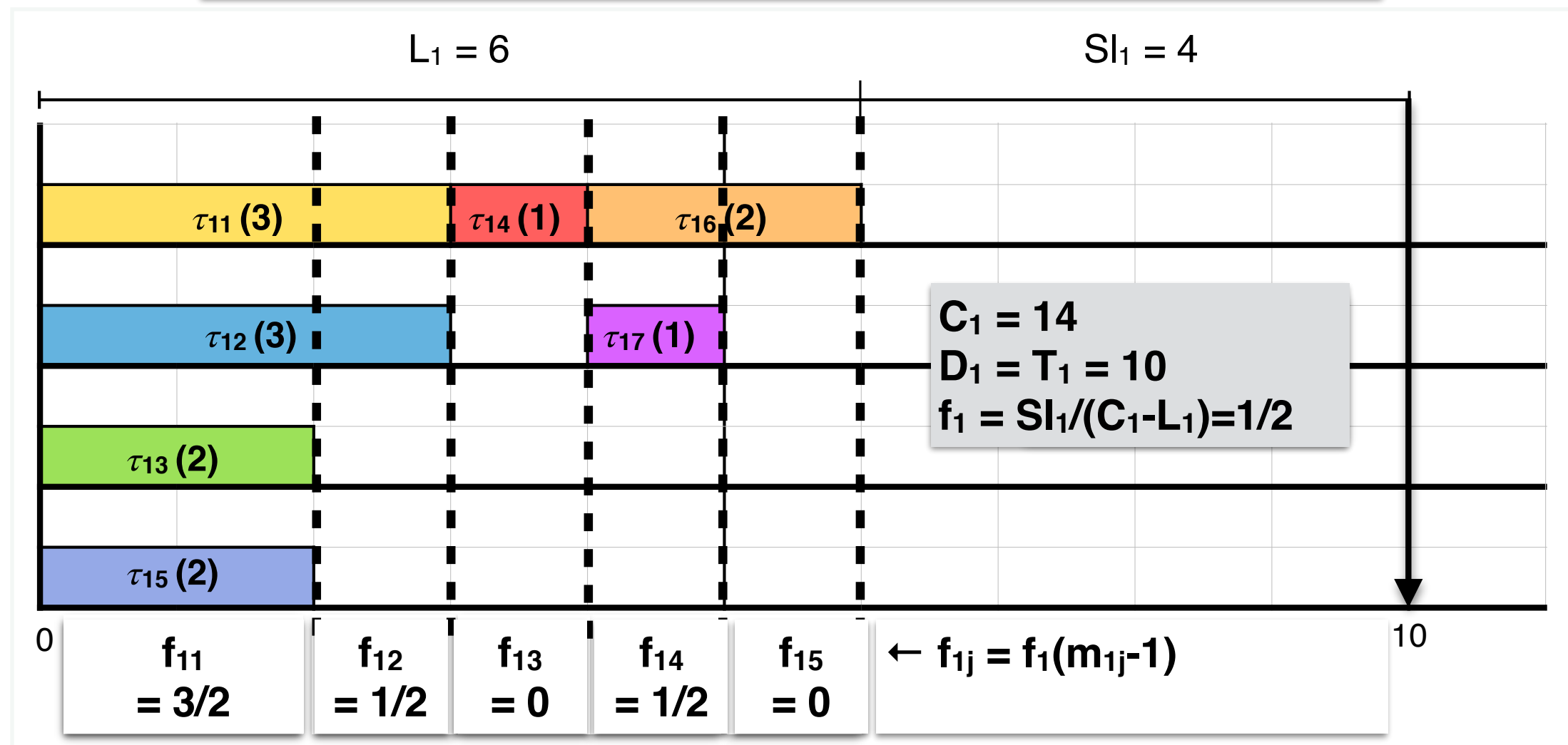


A lot of thread **migration** and **preemptions** are caused.

Solution: fill slack time based on a **Segment-Level**.

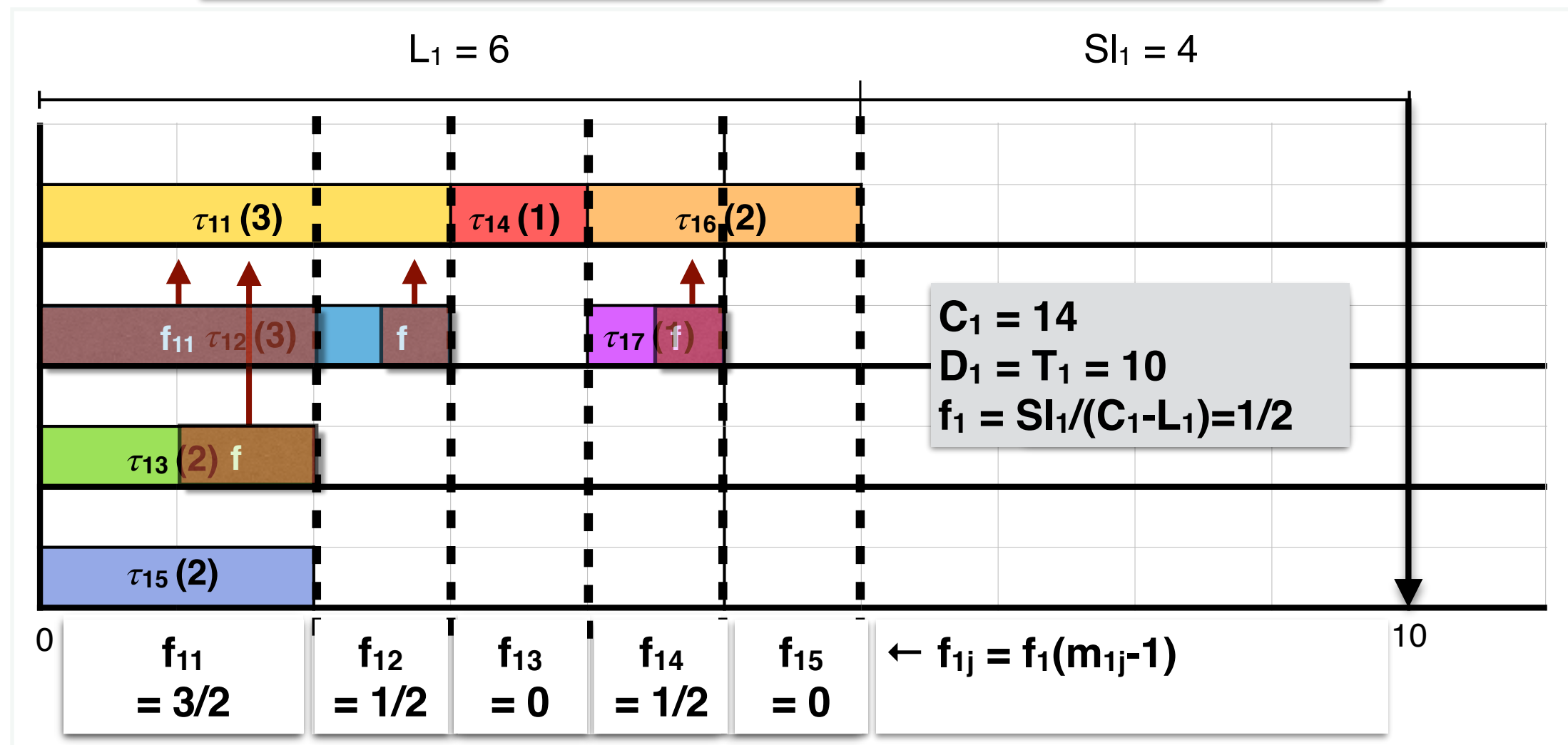
DAG-Str Algorithm

Calculate a segment factor f_{1j} of the DAG task



DAG-Str Algorithm

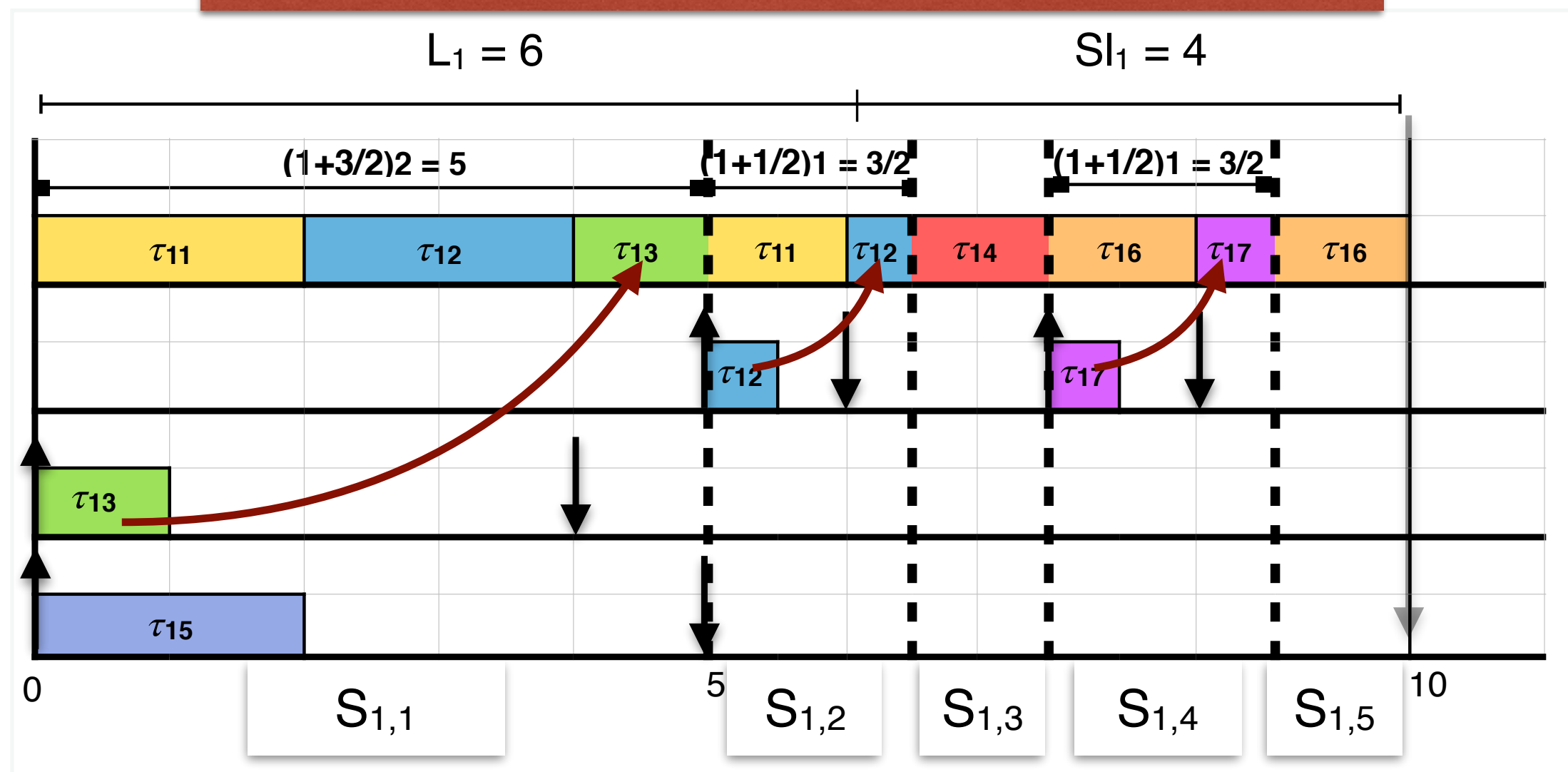
Calculate a segment factor f_{1j} of the DAG task



$(f_{1j} * c_{1j})$ execution units added to **master thread** from each segment S_{1j}
 One thread/segment migrates between processors

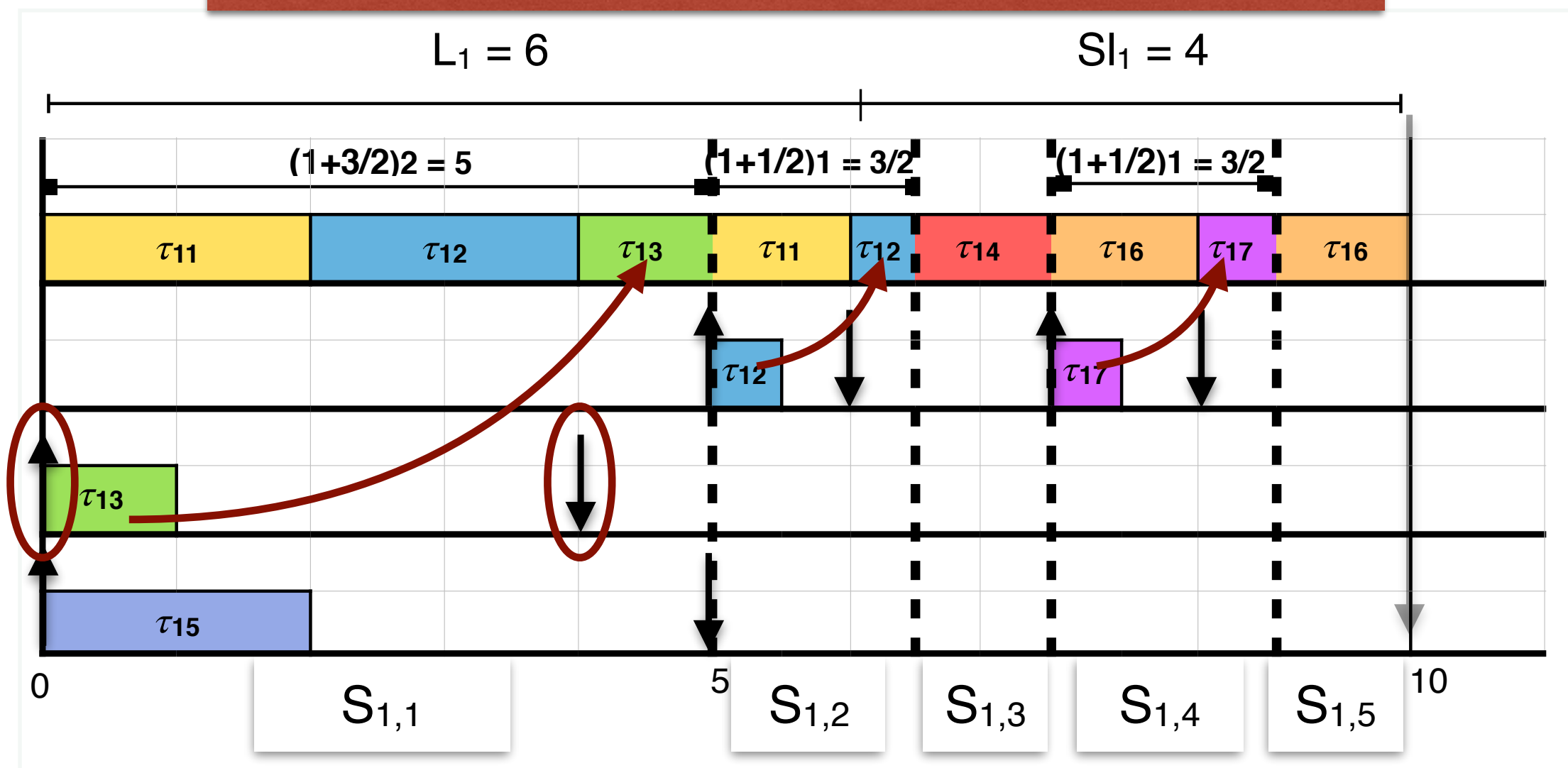
DAG-Str Algorithm

Stretched DAG task



DAG-Str Algorithm

Stretched DAG task



Intermediate **offsets** and **deadlines** are assigned to parallel **threads**

DAG-Str Algorithm

- Results of DAG-Str algorithm when applied on a DAG task whose:
 - Utilization > 1 :
 - Fully-Stretched threads with utilization equal to 1
→ Assigned to dedicated processors.
 - Periodic independent constrained-deadline threads, with intermediate offset and relative deadline.
→ Scheduled using any multiprocessor scheduling algorithm.
 - Utilization $= 1$ → Fully-stretched thread which is assigned to a dedicated processor.
 - Utilization < 1 → Periodic independent implicit-deadline thread scheduled using any multiprocessor algorithm.
- We consider Global Preemptive Earliest-Deadline First (GEDF) Scheduling algorithm.

Resource Augmentation Bound for GEDF

We prove a **resource Augmentation Bound** of global preemptive **EDF** equal to $(3 + \sqrt{5})/2$

for all task sets with $n < \varphi \times \bar{m}$, where:

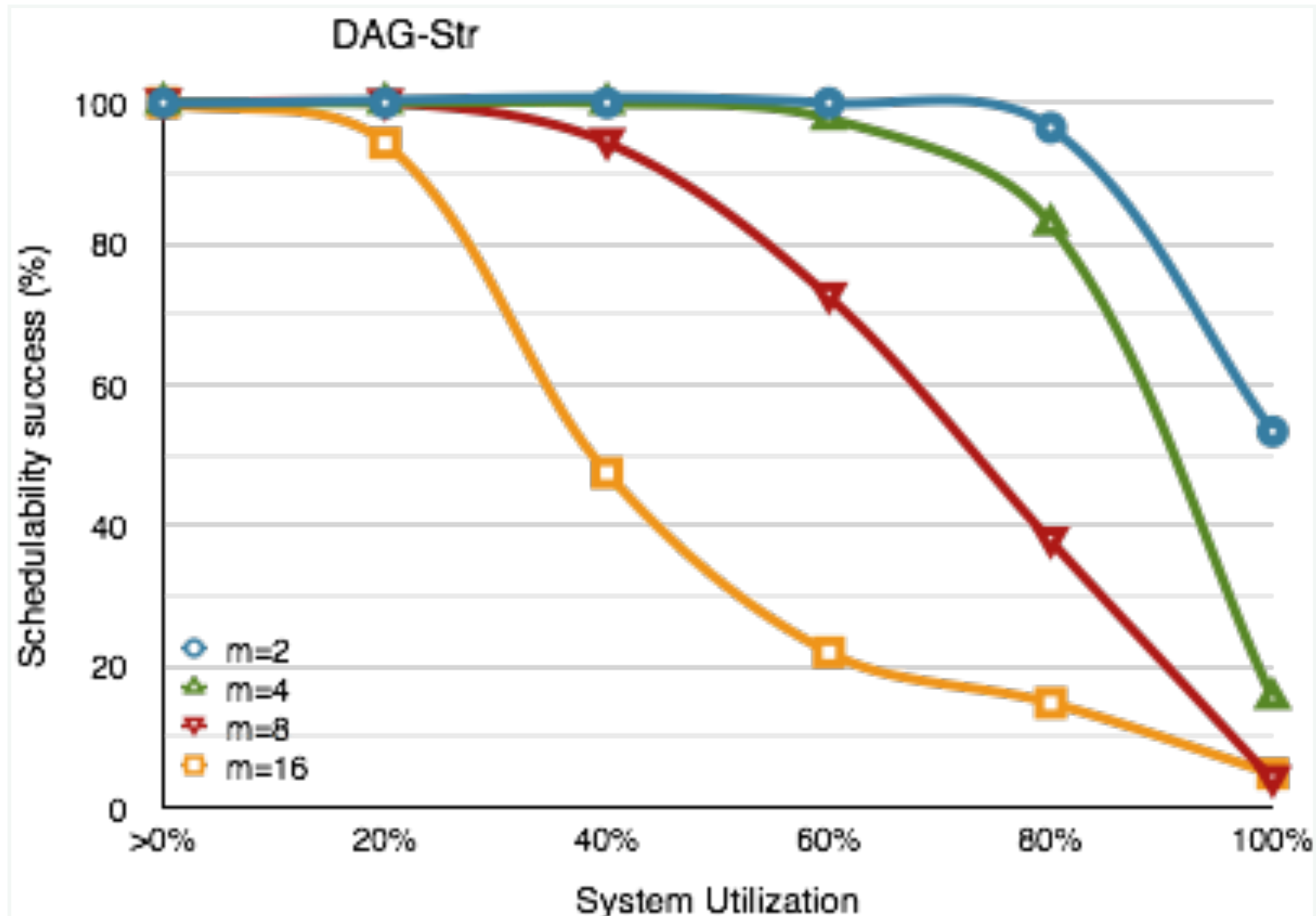
n number of tasks in the set

φ golden ratio where $\varphi = (1 + \sqrt{5})/2$

\bar{m} number of processors after stretching

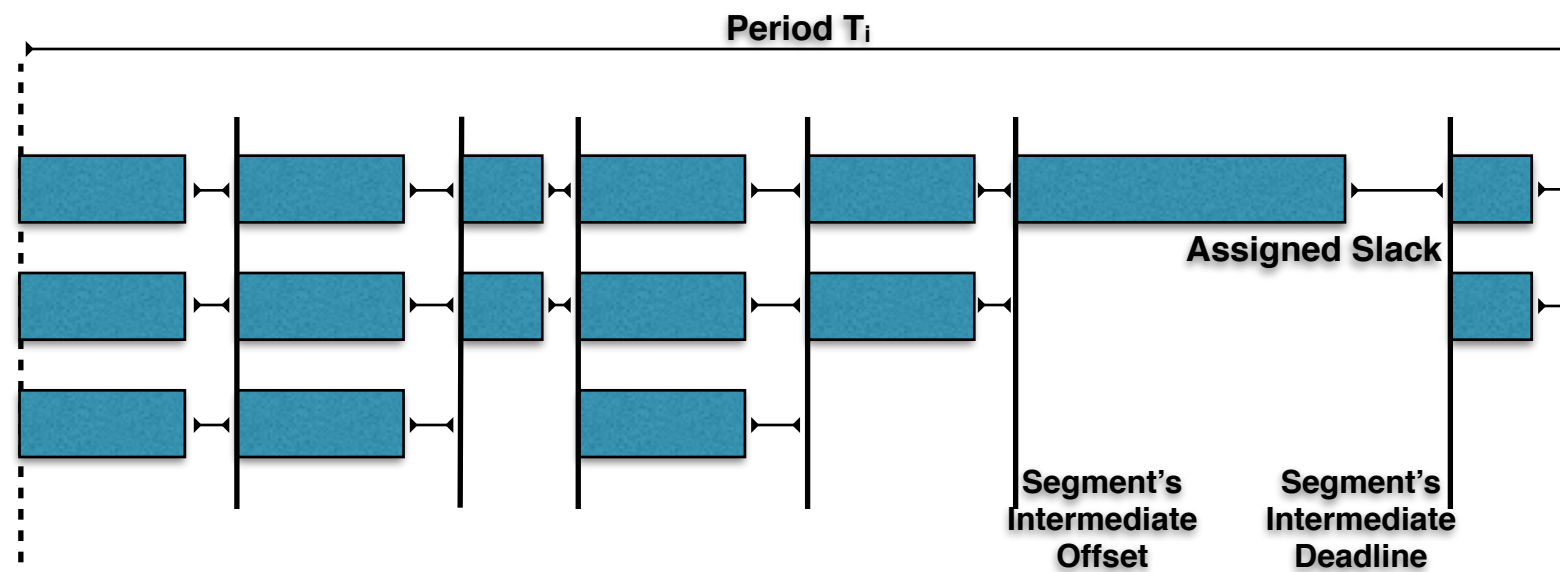
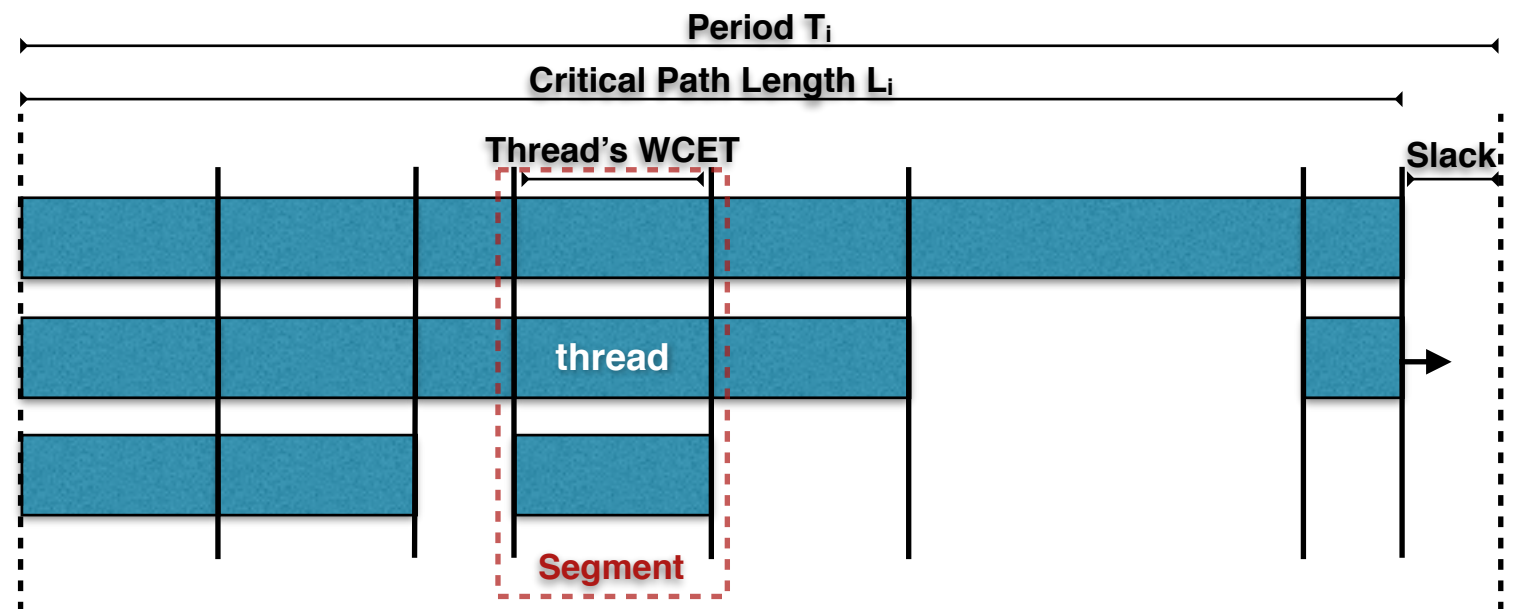
The same value was proved for Global EDF for DAG tasks for large m in [1].

Simulation Results



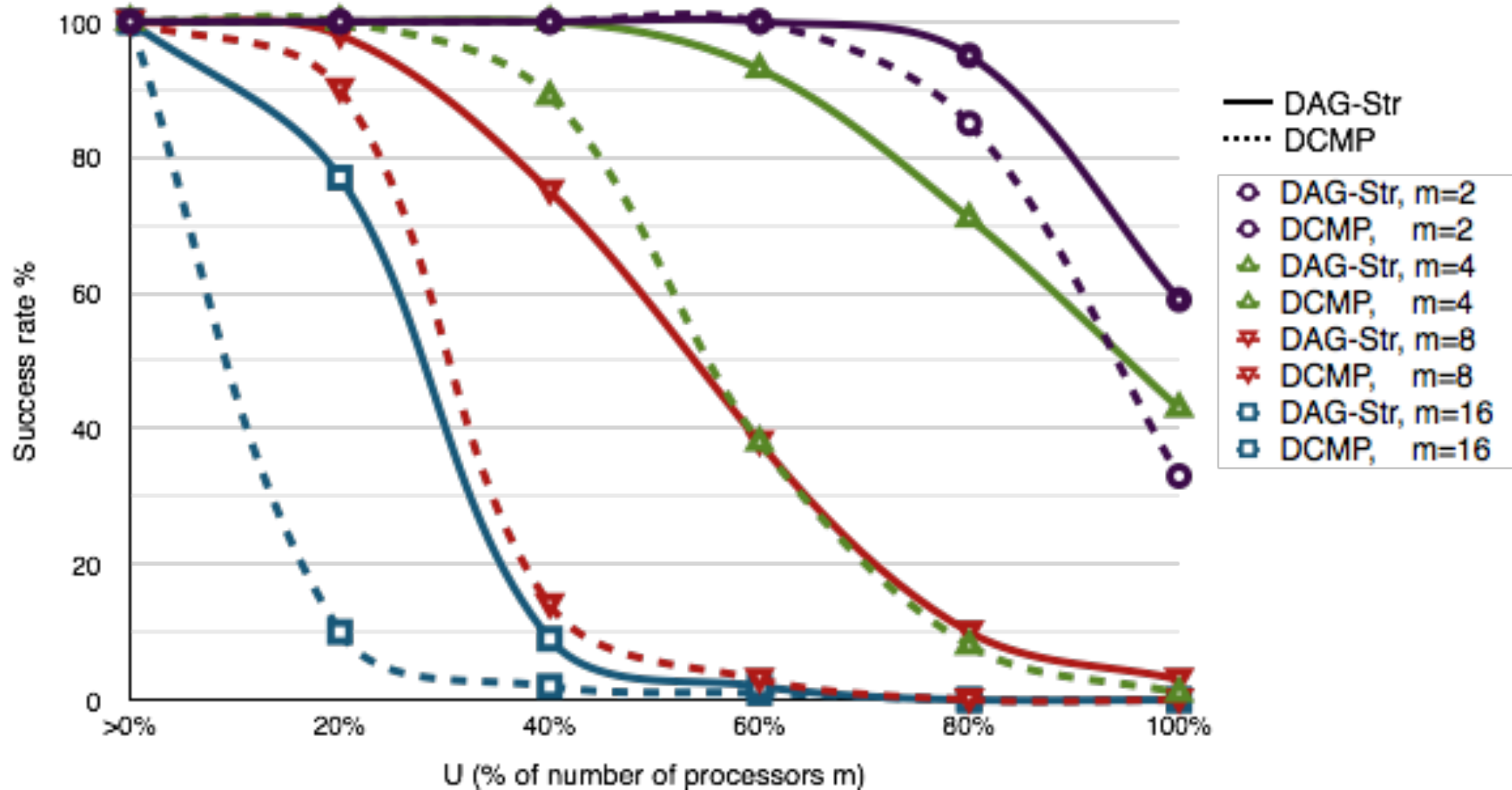
Simulation Results

Compare with
**Decomposition
Algorithm (DCMP)²**
for DAG tasks.

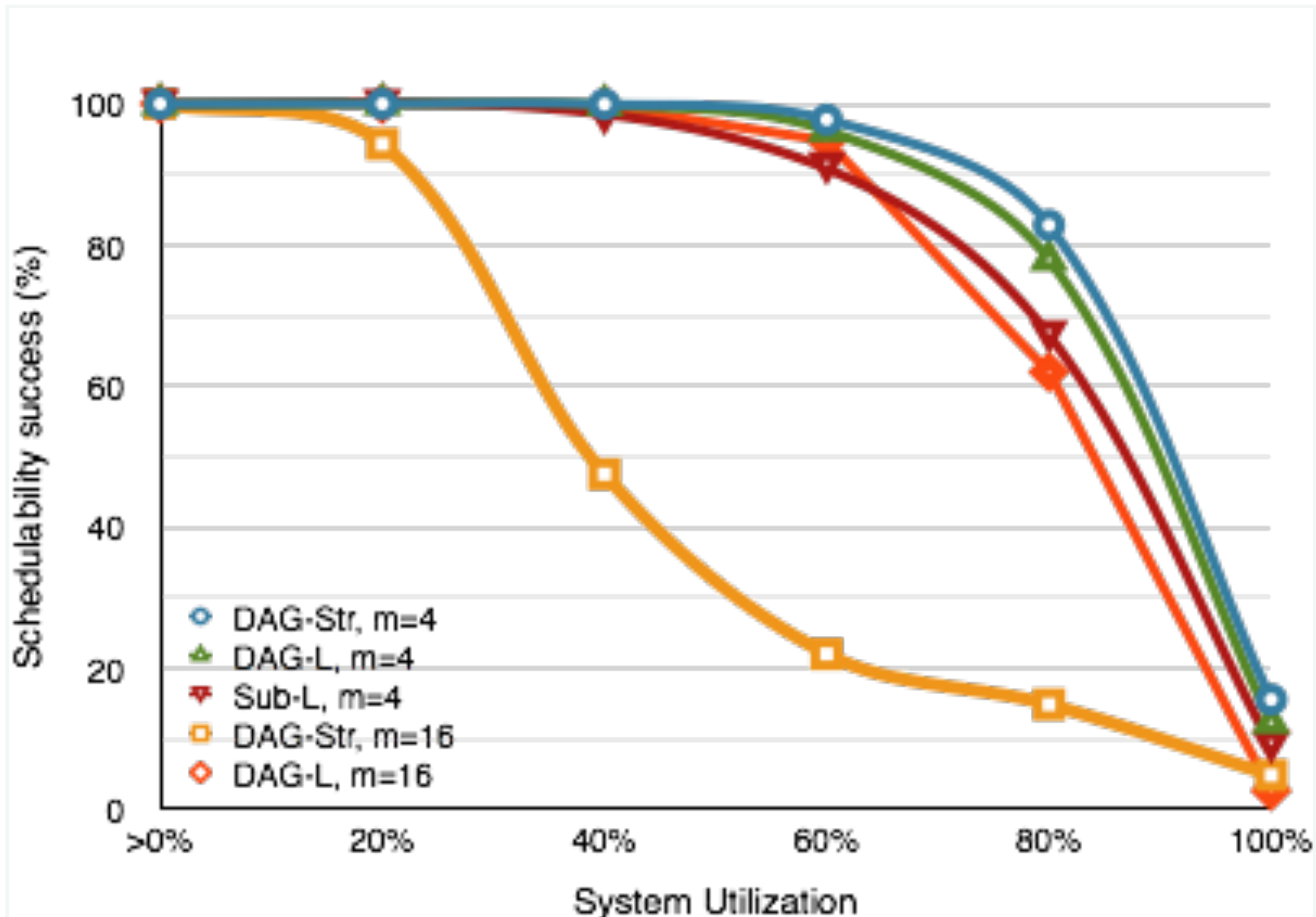


Assigns slack time
for segments based
on a density
threshold

Simulation Results



Simulation Results



Conclusion & Perspectives

- **Conclusions:**

- DAG-Str algorithm which is more general than FJ Stretching algorithm
- Resource Augmentation Bound for GEDF scheduling algorithm.
- Simulation-based evaluations of the stretching algorithm.

- **Perspectives**

- Optimize DAG stretching algorithm to reduce forced migrations and preemptions.
- Analyze Fixed Priority Scheduling Algorithm.

**Thank You
Questions?**